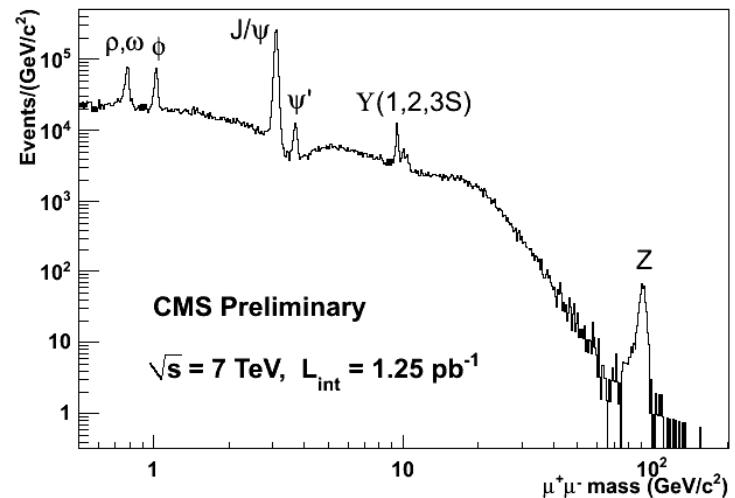


Particles

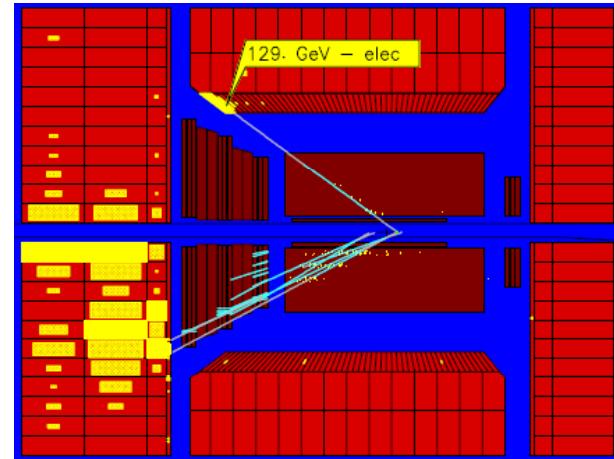
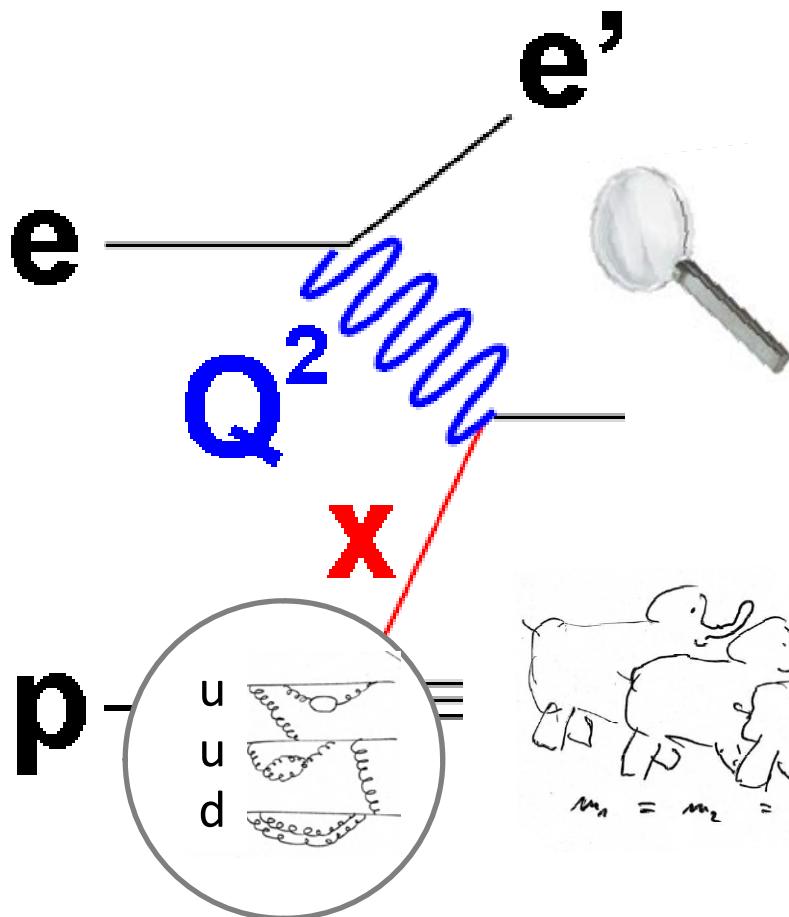


Prof. Dr. Martin Erdmann

RWTH Aachen University

7-Oct-2010

Proton

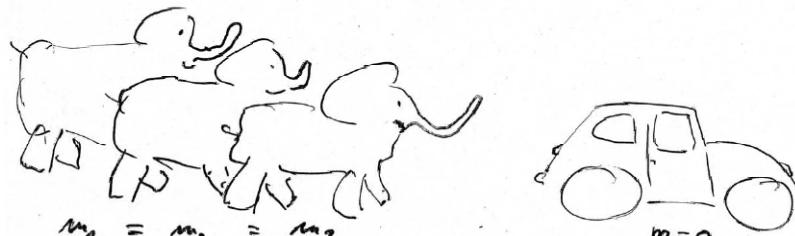


Microscopic
Resolution

$$\lambda = \frac{h}{p} = \frac{h}{\sqrt{Q^2}}$$

Momentum
Fraction

$$x = \frac{p_q}{p_p}$$



Proton Structure Function

$$\Sigma \text{ Spins}=0 \quad \xrightarrow{\downarrow} \quad \text{Rutherford} \quad \text{Quark charge squared}$$

$$\frac{d^2\sigma(eu \rightarrow \leftarrow)}{dx dQ^2} \sim \alpha^2 \frac{1}{Q^4} \frac{4}{9} \frac{1}{x} [x u(x, Q^2)]$$

$u(x, Q^2)$ Wahrscheinlichkeitsdichte

u – Quark im Proton bei (x, Q^2) finden

$x u(x, Q^2)$ Wahrscheinlichkeit = **Partonverteilung**

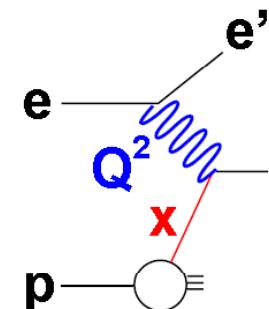
$$\frac{d^2\sigma(eu \rightarrow \rightarrow)}{dx dQ^2} \sim \alpha^2 \frac{1}{Q^4} \frac{4}{9} \frac{1}{x} [x u(x, Q^2)] \underbrace{\cos^4\left(\frac{\theta^*}{2}\right)}$$

$\Sigma \text{ Spins}=1$

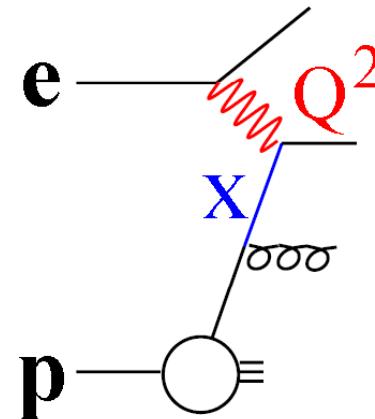
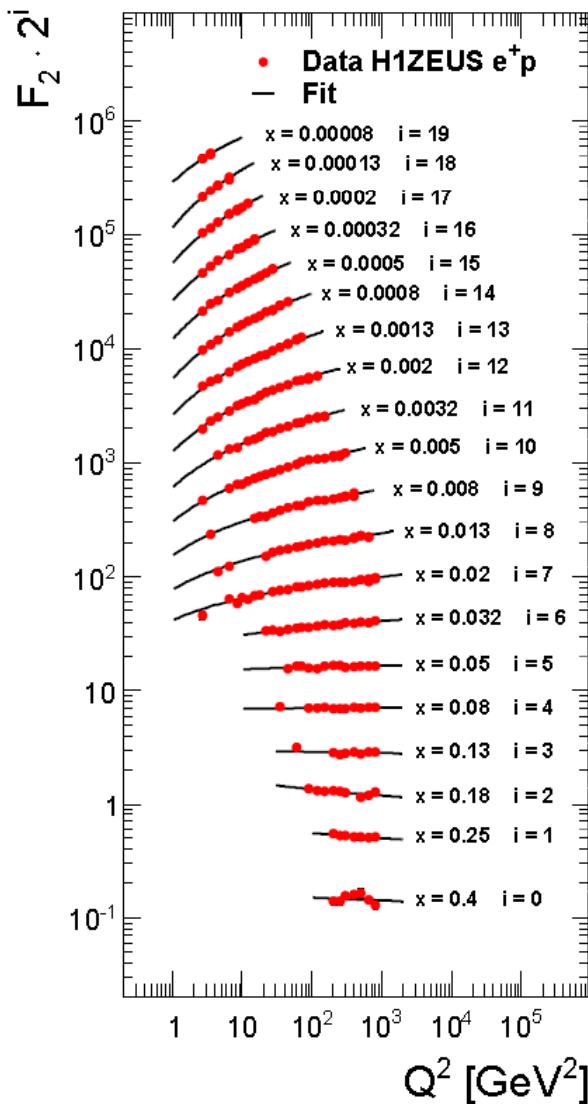
$\frac{d^2\sigma}{dx dQ^2} = \Sigma$ electron-quark cross sections

= Rutherford * Σ Spin term * **Structure Function F_2**

$$F_2(x, Q^2) = \left[\frac{4}{9} x u(x, Q^2) + \frac{1}{9} x d(x, Q^2) + \dots \right]$$



Structure Function: Scaling Violations



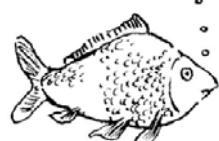
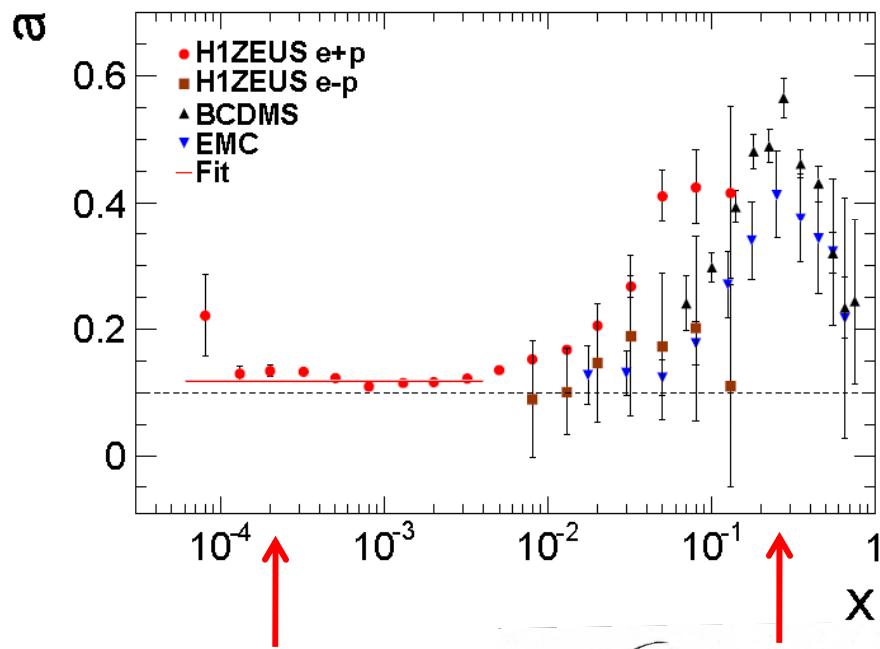
Q^2 -Abh.: QCD-Entwicklungsgleichungen “DGLAP-Gln.”

$$\frac{df_q}{d\ln Q^2} = f_q \text{ (tree-level)} + f_g \text{ (loop corrections)}$$

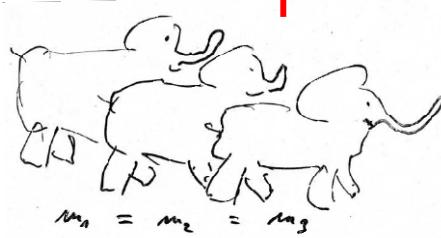
$$\frac{df_g}{d\ln Q^2} = f_q \text{ (loop corrections)} + f_g \text{ (higher-order terms)}$$

Visualizing Quarks in Proton

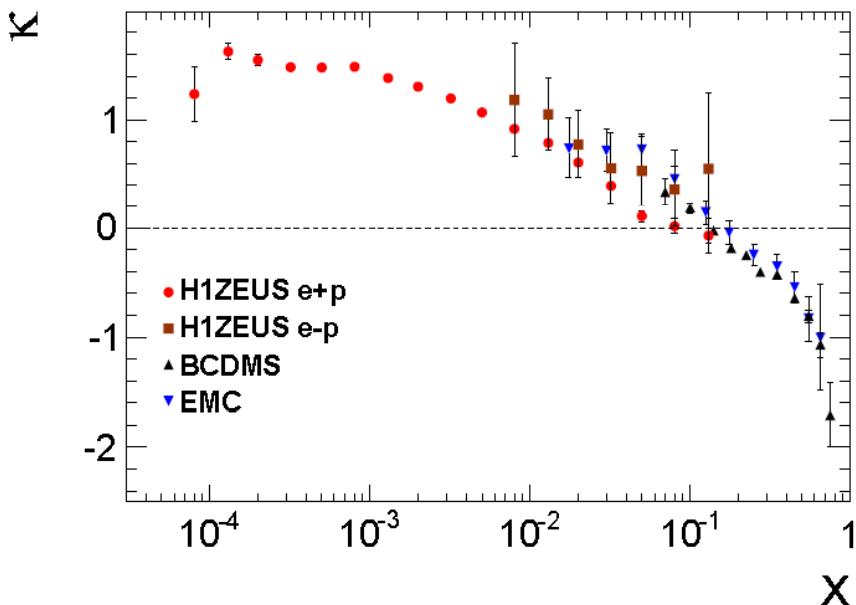
$$F_2(x, Q^2) = a(x) \left[\ln \left(\frac{Q^2}{\Lambda^2} \right) \right]^{\kappa(x)}$$



sea quarks

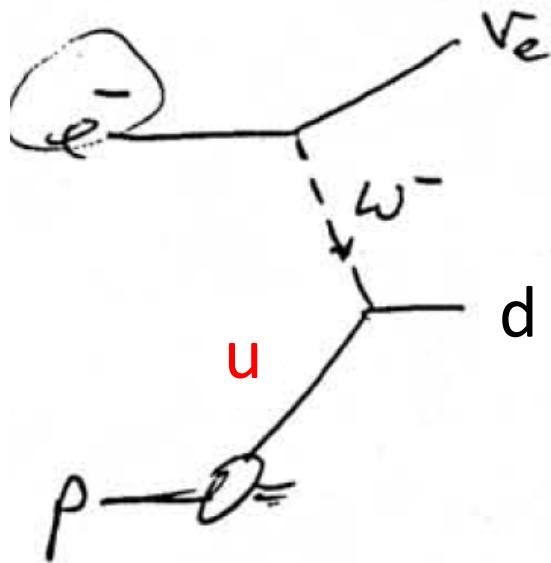


valence quarks

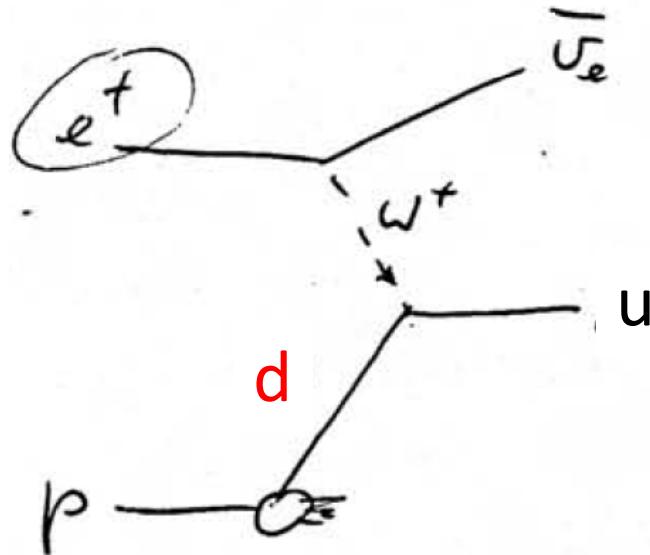


D. Van Aseldonk, M. Erdmann,
T. Klimkovich, M. Nienhaus
DIS 2010, Florence

Quark Flavours in Proton



quark needs
positive charge



quark needs
negative charge

cross sections imply valence quarks of **proton=uud**

Nucleon Resonances

name	Particle	L_{2I-2J}	status	$N\pi$	$N\eta$	ΛK	ΣK	$\Delta\pi$	$N\rho$	$N\gamma$
Mass [MeV]	$N(939)$	P_{11}	****							
	$N(1440)$	P_{11}	****	****	*			***	*	***
	$N(1520)$	D_{13}	****	****	***			****	****	****
	$N(1535)$	S_{11}	****	****	****			*	**	***
		$\Delta(1232)$	---	****	****	F				****
		$\Delta(1600)$	P_{33}	***	***	O		***	*	**
		$\Delta(1620)$	S_{31}	****	****	r		****	****	***
		$\Delta(1700)$	D_{33}	****	****	b	*	***	**	***

Δ BARYONS ($S=0, I=3/2$)

$$\Delta^{++} = uuu, \quad \Delta^+ = uud, \quad \Delta^0 = udd, \quad \Delta^- = ddd$$

Δ^{++} antisymmetric wave function ?



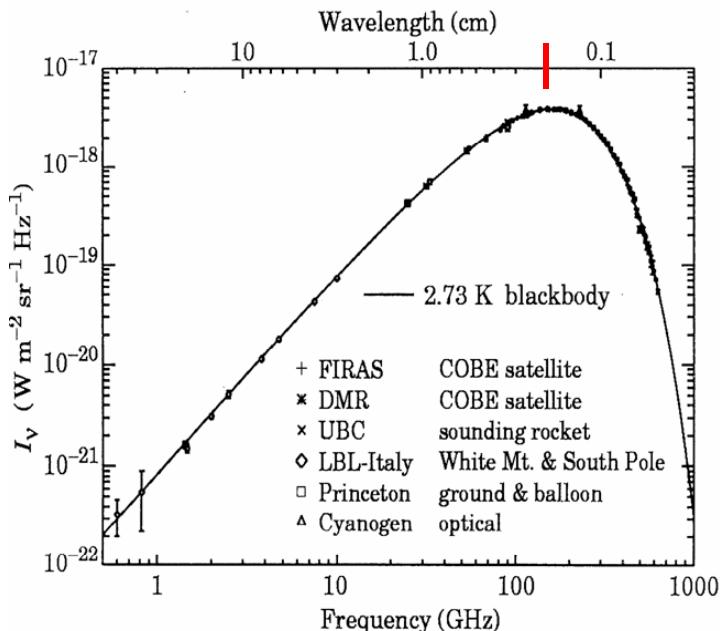
Quarks: 3 colors

Photon-Proton-Interactions

Photons: cosmic microwave background

$$T = 2.728 \pm 0.004 \text{ K}$$

Target density: 380 Photonen pro cm³



$$\begin{aligned} E_\gamma &= \frac{2 \pi \hbar c}{\lambda} = \frac{6 * 0.2 \text{ GeV fm}}{0.2 \text{ cm}} \\ &= 6 \cdot 10^{-4} \text{ eV} \end{aligned}$$

Δ – Resonance: need Proton with

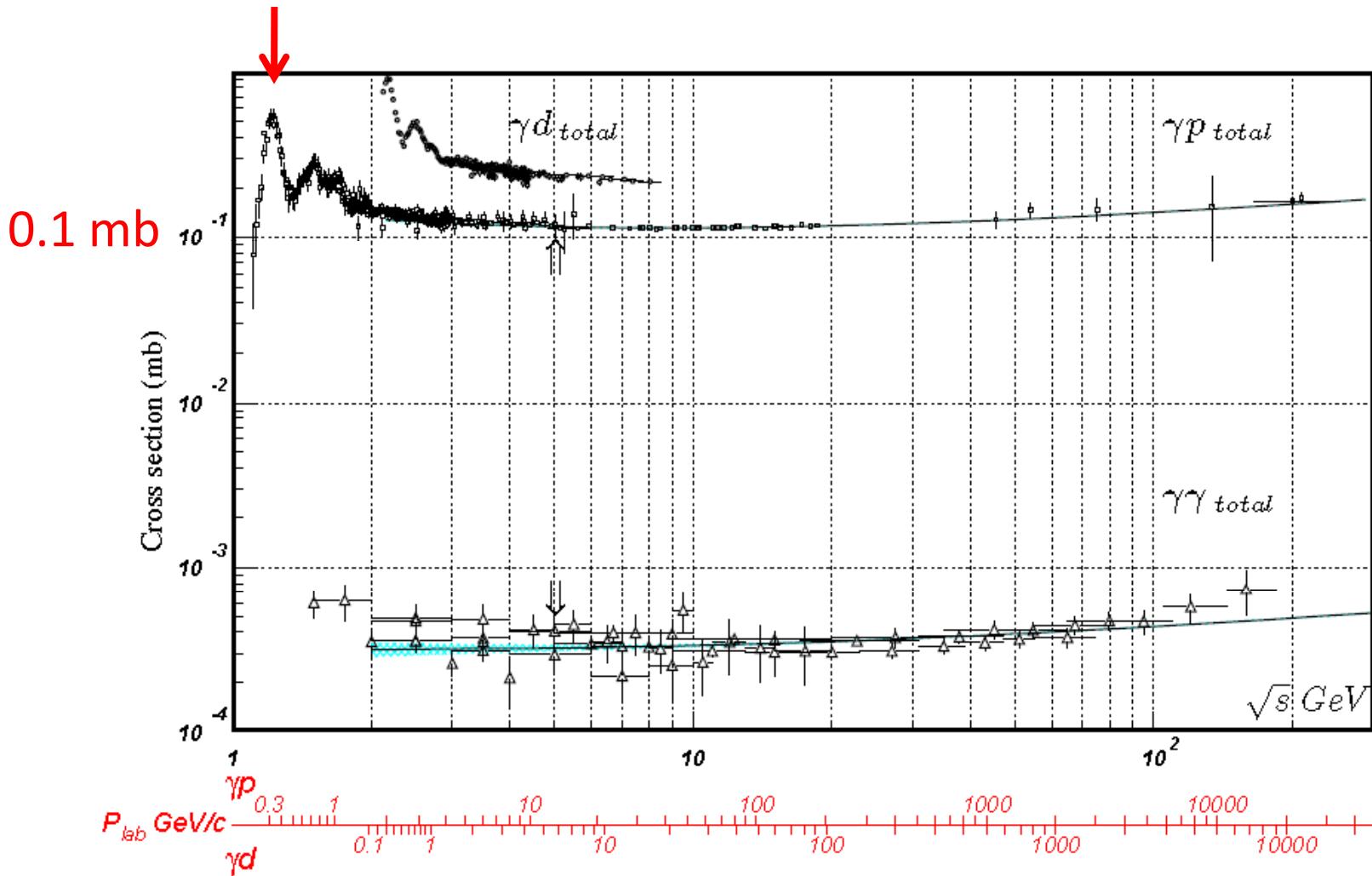
$$\begin{aligned} p_p + p_\gamma &= p_\Delta \\ \left(\vec{p}_p c + \vec{p}_\gamma c \right) &= \left(m_\Delta c^2 \ 0 \right) \end{aligned}$$

$$E_p > 5 \cdot 10^{19} \text{ eV}$$

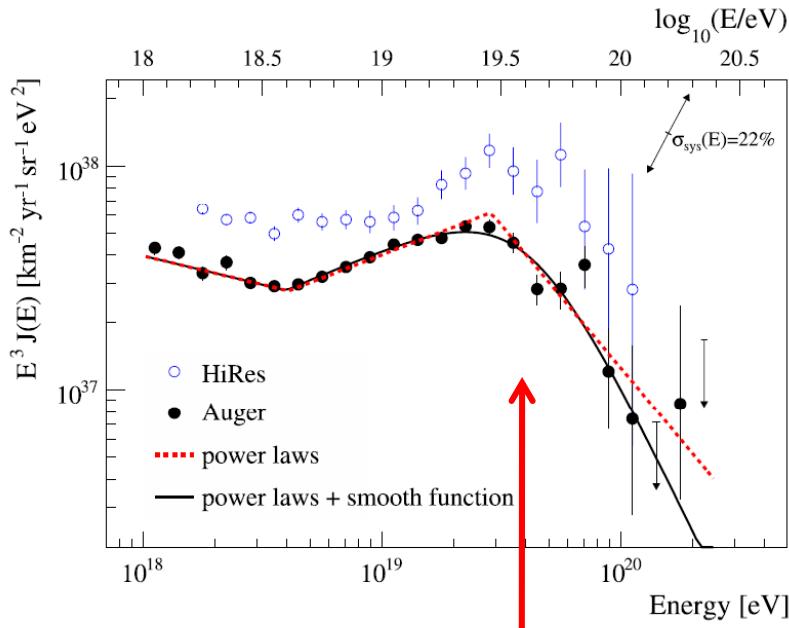
Greisen–Zatsepin–Kuzmin
(GZK-cutoff)

Cross Section γp Interactions

Δ Resonance we know the cross section



Cosmic Ray Energy Spectrum



Proton from Δ Decay
carries less energy

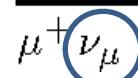
$\Delta(1232)$ DECAY MODES



Fraction (Γ_i/Γ)

100 %

π^+ DECAY MODES



„GZK Neutrinos“

Fraction (Γ_i/Γ)

[b] $(99.98770 \pm 0.00004) \%$

π^0 DECAY MODES



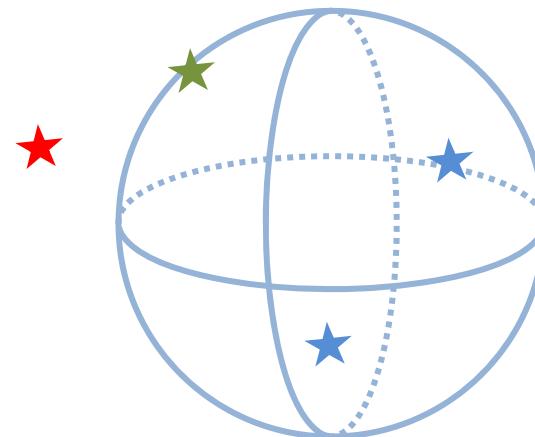
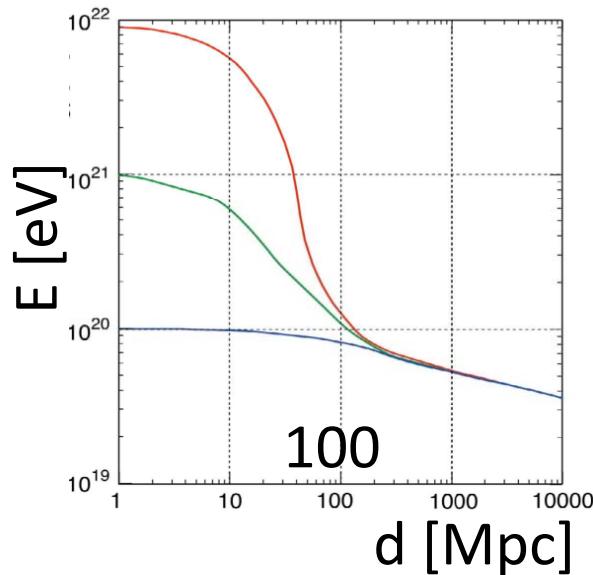
„GZK Photons“

Fraction (Γ_i/Γ)

$(98.823 \pm 0.034) \%$

GZK Horizon

Expected energy loss

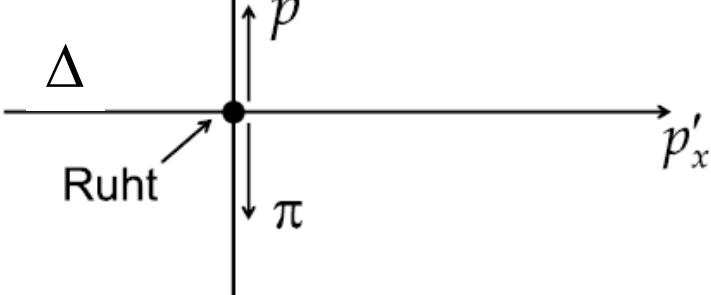


Expect sources of ultra high energy cosmic rays
within a 100 Mpc sphere from earth

Δ Decay

Decay Momenta

$$p'_y = \frac{(m_\Delta^2 - m_p^2)c}{2m_\Delta}$$



Decay Angles

Pion Lab

$$\begin{pmatrix} E \\ p_x c \\ p_y c \\ p_z c \end{pmatrix} = \begin{pmatrix} \gamma & \gamma\beta & 0 & 0 \\ \gamma\beta & \gamma & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} E' \\ 0 \\ p'_y c \\ 0 \end{pmatrix}$$

$$\gamma = \frac{E_\Delta}{m_\Delta c^2} \quad \beta = \sqrt{1 - \frac{1}{\gamma^2}}$$

Δ kinematics

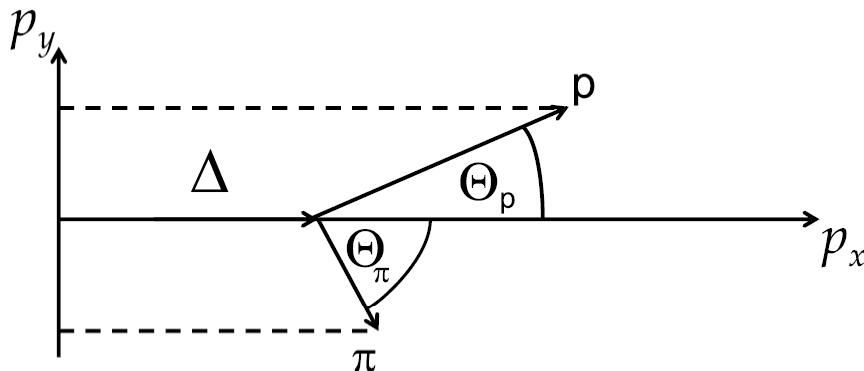
Pion CMS

Proton (heavy) reflects the original Δ direction

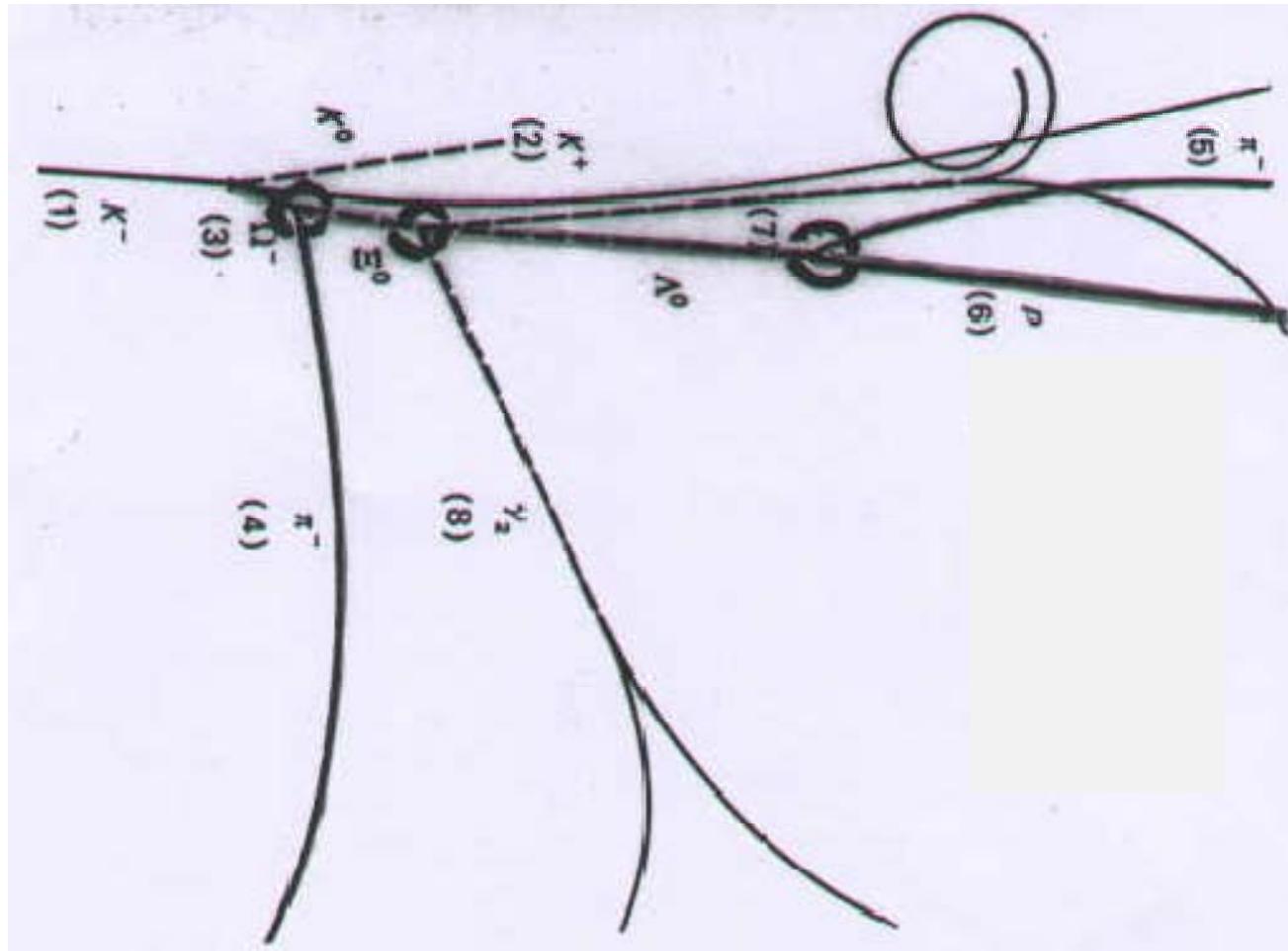
$$\tan \Theta_p = \frac{1}{\gamma \sqrt{\frac{m_p^2 c^2}{p'^2 c^2} + 1}} \approx 0$$

Pion (~massless) has angle

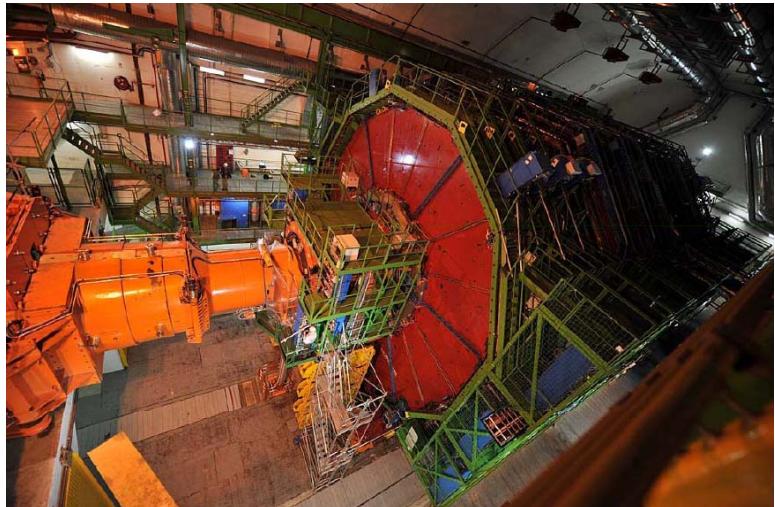
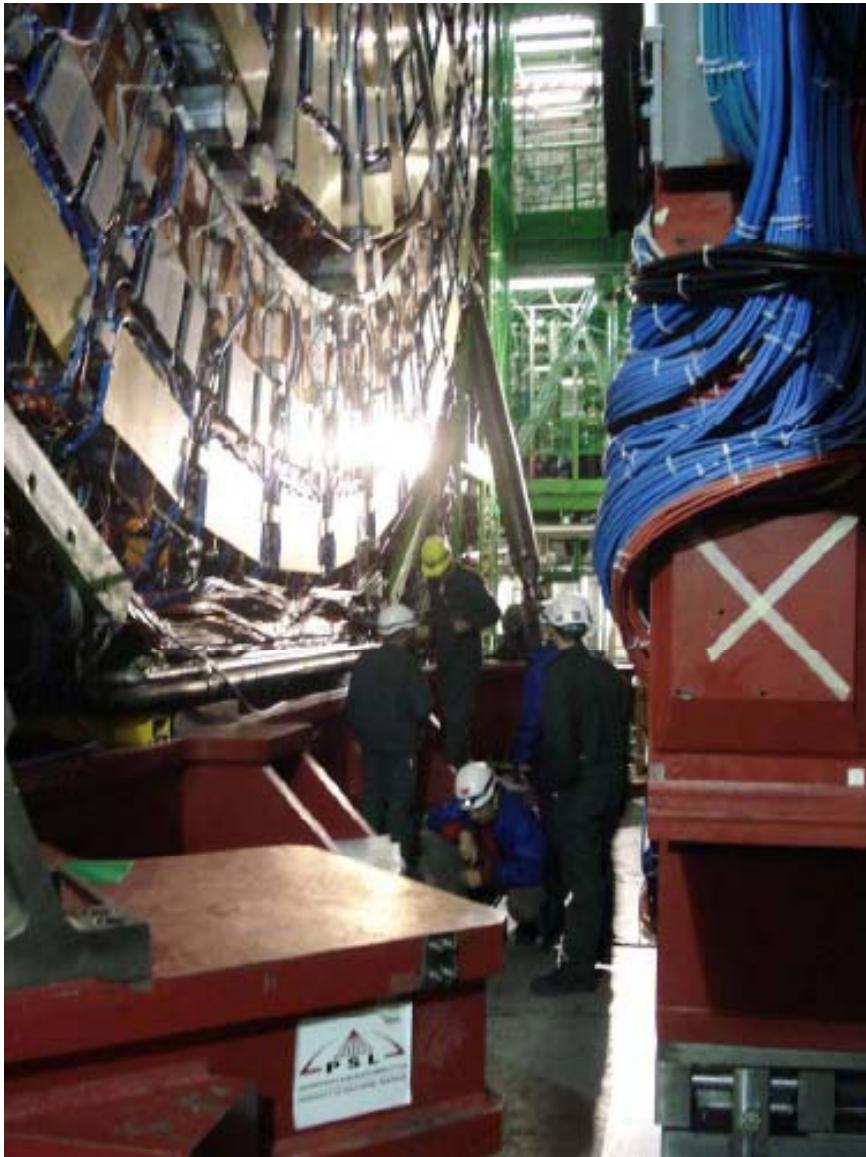
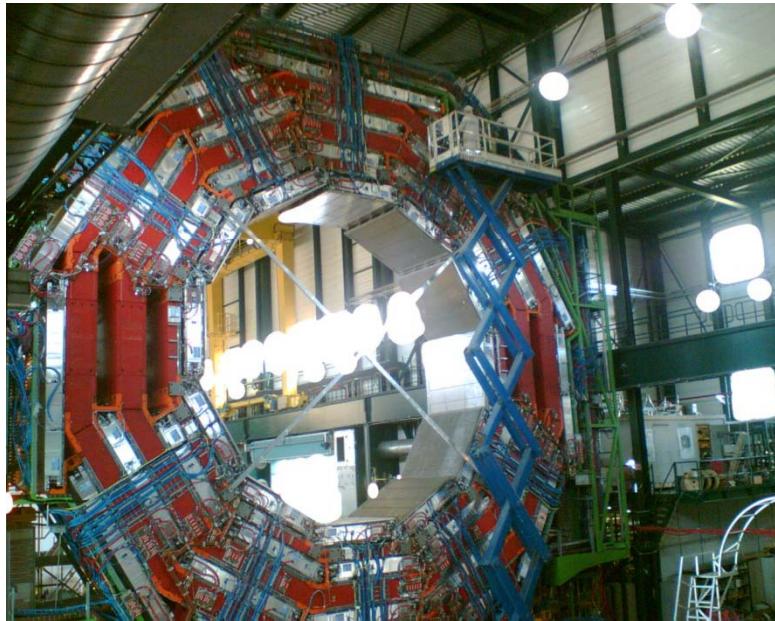
$$\tan \Theta_\pi \approx \frac{1}{\gamma}$$



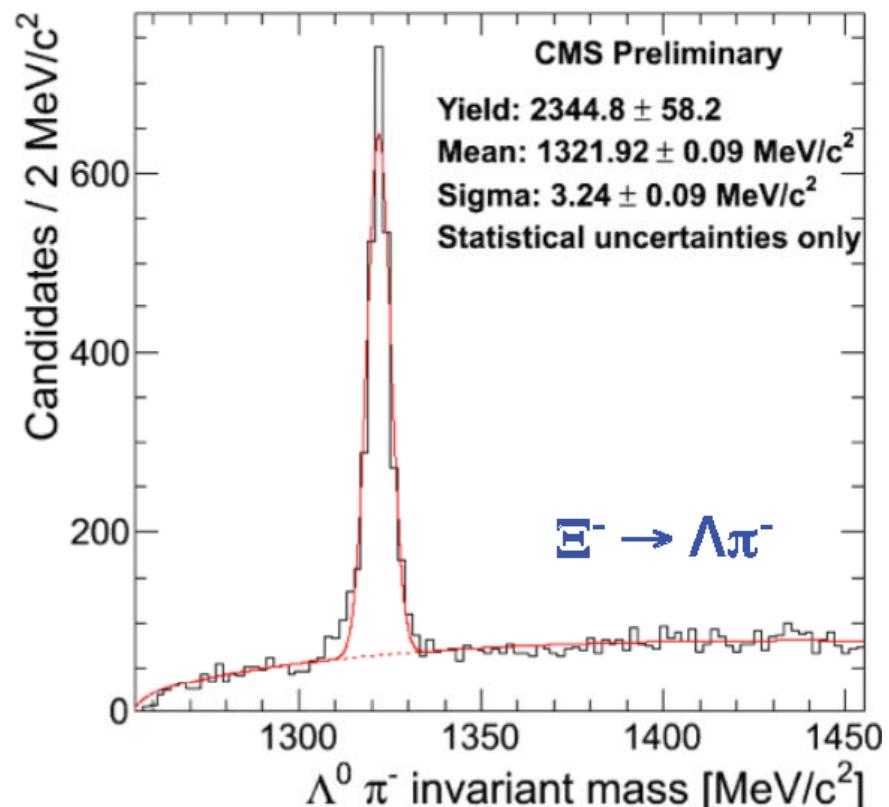
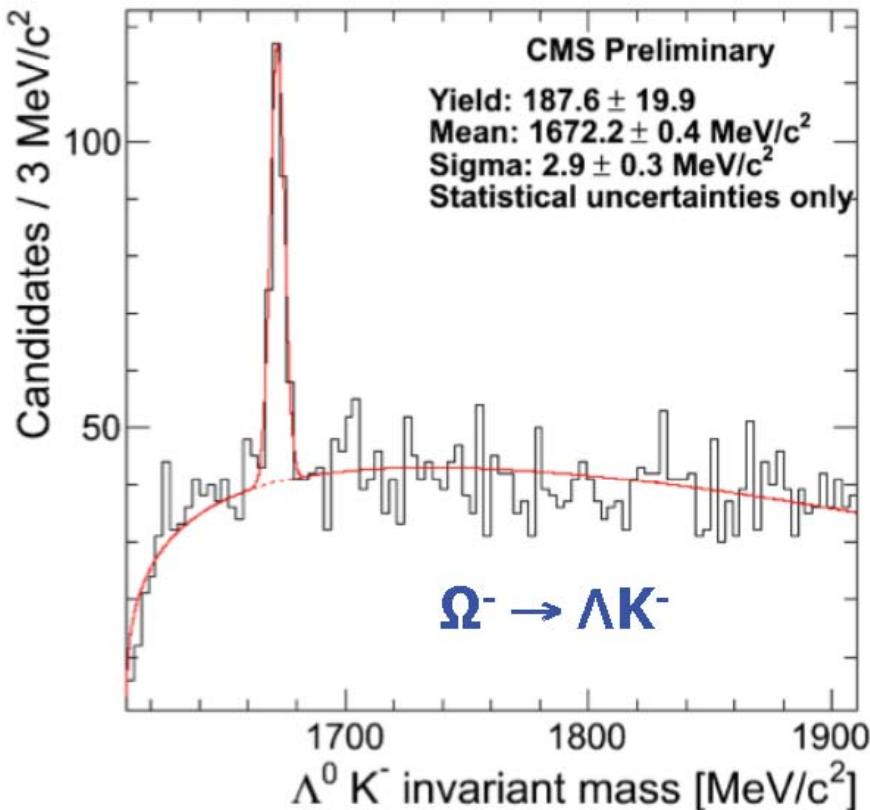
Heavy Particle Preserves Direction



Compact Myon Solenoid at the LHC

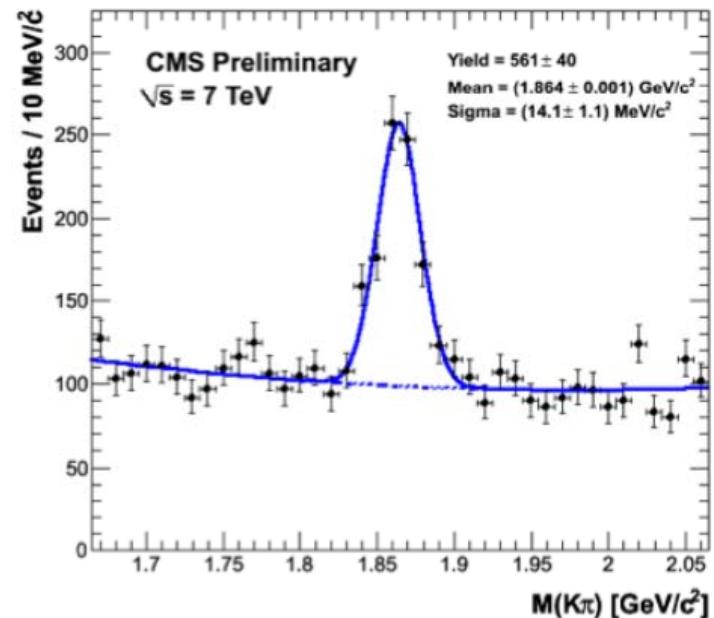
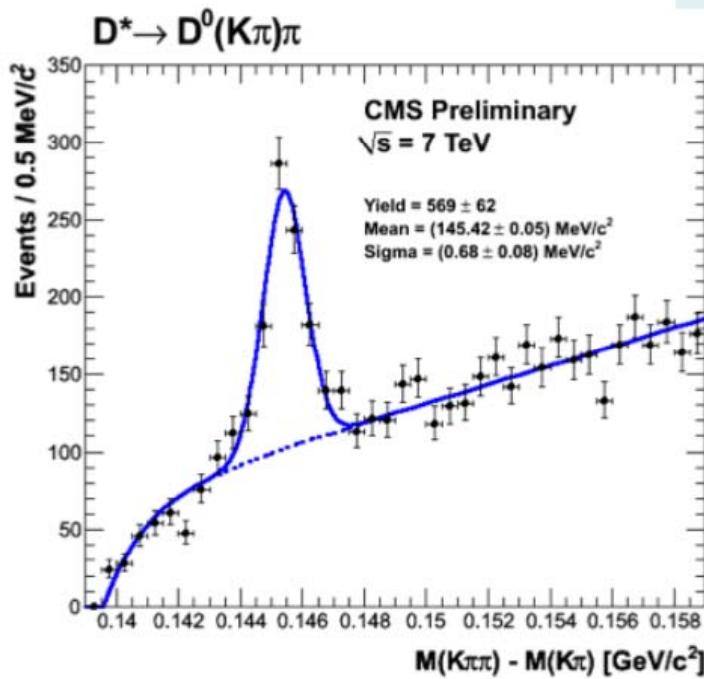


CMS: Classic Baryons



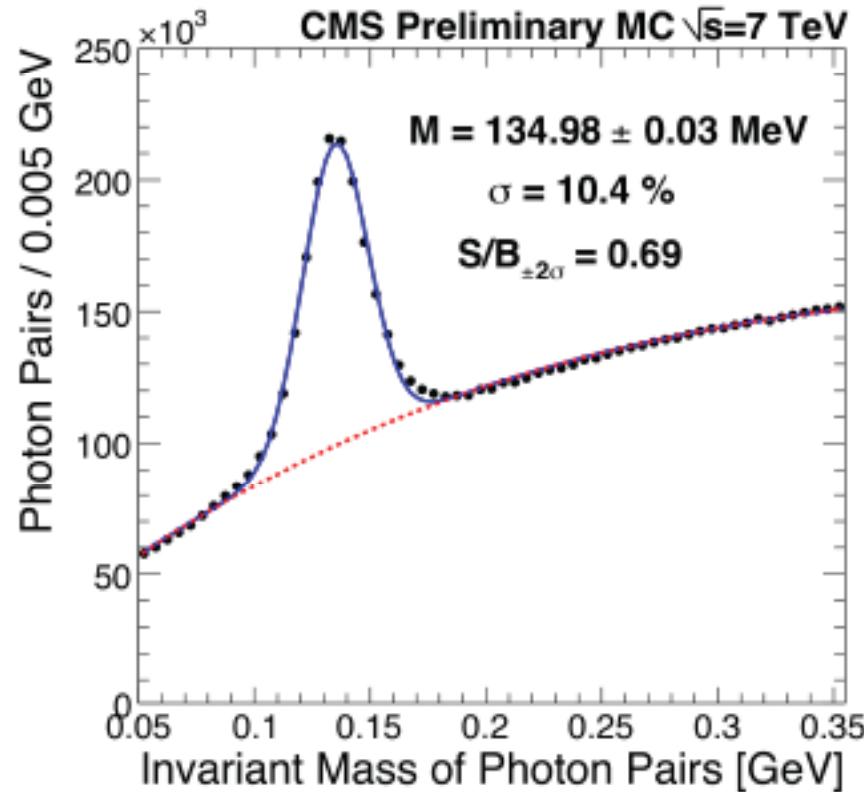
Silicon tracker

CMS: Charm



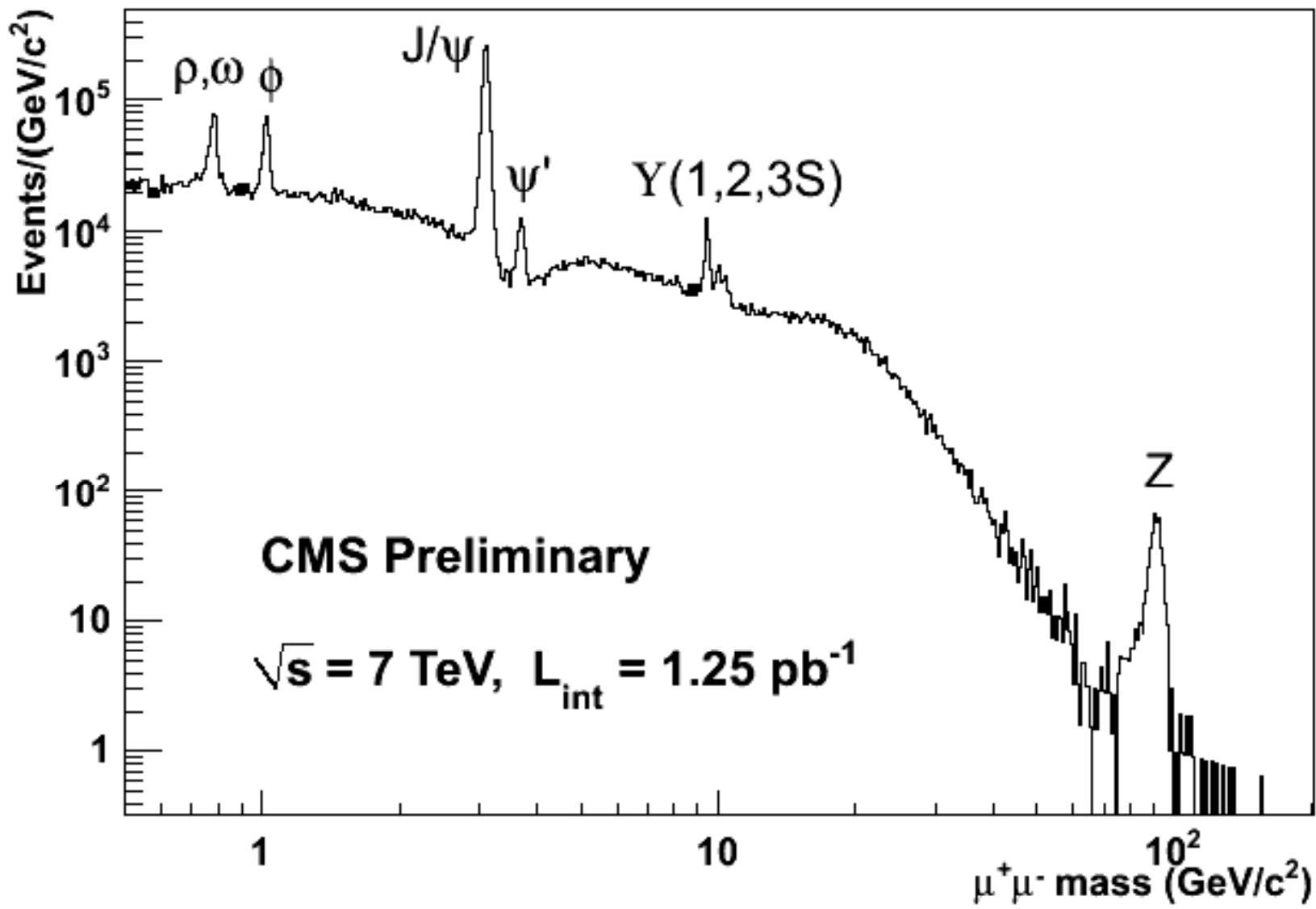
Silicon tracker

CMS: $\pi_0 \rightarrow 2 \gamma$



Electromagnetic calorimeter

CMS: Myon Detector



Summary

- Proton is well understood
- LHC experiments re-discover the particle zoo
- Δ Resonance: limits observed cosmic ray energy spectrum
- GZK horizon limits the source candidates to within 100 Mpc